

Appendix to Deflation: Prevention and Cure

A Simple Model of Aggregate Demand^{* **}

14-07-2003

Willem H. Buiter

European Bank for Reconstruction and Development

This Appendix provides some technical background for Buiter [2003].

Households

First, I consider the individual consumption behaviour of households that operate in perfect financial markets and can borrow freely against the security of their future disposable labour income. In the body of the paper these are called permanent income consumers. Next aggregate consumption is derived on the assumption that all consumers are permanent income consumers. The final step is to derive aggregate consumption behaviour when a constant fraction of households is constrained to consume their disposable (after-tax) labour income in each period. The second category of consumers are called ‘Keynesian’ consumers in the body of the paper.

A representative member of the generation born in period $t-s$, $s \geq 0$, maximizes at time t the expected utility of life-time sequences of consumption of domestic goods, imported goods and real money balances. The objective functional $v_{t-s,t}$ is given in equations (1), (2) and (3). The period household budget identity is given in equations (7) or (9) and the household solvency constraint in (10). There is a constant (that is, both time-independent and age-independent) probability of

* © Willem H. Buiter 2003

**The views and opinions expressed are those of the author and do not represent the official views and opinions of the European Bank for Reconstruction and Development.

survival till the next period, given by $\frac{1}{1+\mathbf{d}}$, $\mathbf{d} \geq 0$; \mathbf{d} can be thought of as the death rate. The pure subjective rate of time preference is $\mathbf{r} > 0$. Uncertainty about the time of death is the only uncertainty in the model, and its only effect on the objective functional is to raise the effective subjective discount factor from $1+\mathbf{r}$ to $(1+\mathbf{r})(1+\mathbf{d})$. Period felicity of a household born at time $t-s$, $s \geq 0$ and surviving at time t is given by a constant intertemporal elasticity of substitution function $z_{t-s,t}$, where z is a CES function of a composite consumption good, $\tilde{c}_{t-s,t}$, and end-of-period real money balances, $M_{t-s,t} / \tilde{P}_t$. The nominal stock of base money held by the generation $t-s$ household at the end of period t is $M_{t-s,t}$ and \tilde{P} is the money price of the composite consumption good. The composite consumption good is itself a CES function of consumption of domestic goods, $c_{t-s,t}^H$ (with money price P) and consumption of imported goods $c_{t-s,t}^F$ (with domestic money price SP^* , where P^* is the foreign currency price of imports and S is the nominal spot exchange rate). The intertemporal substitution elasticity is denoted \mathbf{s} .

For $\mathbf{r} > 0; \mathbf{d} \geq 0; \mathbf{s} > 0, \mathbf{s} \neq 1$

$$v_{t-s,t} = \sum_{j=t}^{\infty} \left(\frac{1}{(1+\mathbf{r})(1+\mathbf{d})} \right)^{j-(t-1)} \frac{\mathbf{s}}{\mathbf{s}-1} (z_{t-s,j})^{\frac{\mathbf{s}-1}{\mathbf{s}}} \quad (1)$$

For $\mathbf{s}=1$

$$v(t-s,s) = \sum_{j=t}^{\infty} \left(\frac{1}{(1+\mathbf{r})(1+\mathbf{d})} \right)^{j-(t-1)} \ln z_{t-s,j}$$

For $0 < \mathbf{a} < 1; \mathbf{j} > 0; \mathbf{j} \neq 1$

$$z_{t-s,j} = \left[\mathbf{a}^{\frac{1}{j}} \left(\tilde{c}_{t-s,j} \right)^{\frac{j-1}{j}} + (1-\mathbf{a})^{\frac{1}{j}} \left(\frac{M_{t-s,j}}{\tilde{P}_j} \right)^{\frac{j-1}{j}} \right]^{\frac{j}{j-1}} \quad (2)$$

For $\mathbf{j} = 1$

$$z(t-s, j) = \left(\tilde{c}_{t-s,j} \right)^{\mathbf{a}} \left(\frac{M_{t-s,j}}{\tilde{P}_j} \right)^{1-\mathbf{a}}$$

For $0 < \mathbf{h} \leq 1; \mathbf{q} > 0; \mathbf{q} \neq 1$

$$\tilde{c}_{t-s,j} = \left(\mathbf{h}^{\frac{1}{q}} \left(c_{t-s,j}^H \right)^{\frac{q-1}{q}} + (1-\mathbf{h})^{\frac{1}{q}} \left(c_{t-s,j}^F \right)^{\frac{q-1}{q}} \right)^{\frac{q}{q-1}} \quad (3)$$

For $\mathbf{q} = 1$

$$\begin{aligned} \tilde{c}_{t-s,j} &= (c_{t-s,j}^H)^{\mathbf{h}} (c_{t-s,j}^F)^{1-\mathbf{h}} \\ \tilde{P} &= \left(\mathbf{h} P^{1-\mathbf{q}} + (1-\mathbf{h}) (SP^*)^{1-\mathbf{q}} \right)^{\frac{1}{1-\mathbf{q}}} \quad \text{if } \mathbf{q} \neq 1 \\ \tilde{P} &= P^{\mathbf{h}} (SP^*)^{1-\mathbf{h}} \quad \text{if } \mathbf{q} = 1 \end{aligned} \quad (4)$$

Households have access to four stores of value, domestic base money, M , with nominal interest rate i_M , one-period debt denominated in domestic currency, B , with nominal interest rate i , one-period debt denominated in foreign currency, B^* , with nominal interest rate i^* and equity, claims to the domestic capital stock. The quantity of domestic capital held by the household is denoted K and the domestic currency price of a claim to one unit of domestic capital is P^K . A unit of capital purchased for a price P_t^K in period t entitles one to a nominal dividend of Ω_{t+1} in period $t+1$, plus

the right to resell the undepreciated part of the capital at unit price P_{t+1}^K . The proportional rate of depreciation of the capital stock is \mathbf{x} . The rate of inflation of the

composite good price $\tilde{\mathbf{p}}$ is defined as $\tilde{\mathbf{p}}_t \equiv \frac{\tilde{P}_j}{\tilde{P}_{j-1}} - 1$, and the one-period domestic real

interest rate in terms of the composite consumption good \tilde{r} is defined as

$1 + \tilde{r}_j \equiv \frac{1 + i_j}{1 + \tilde{\mathbf{p}}_j}$. We also define the real values (in terms of the composite

consumption good) of the four asset stocks as $\tilde{m}_{t-s,j} \equiv \frac{M_{t-s,j}}{\tilde{P}_j}$, $\tilde{b}_{t-s,j} \equiv \frac{B_{t-s,j}}{\tilde{P}_j}$,

$\tilde{b}_{t-s,j}^* \equiv \frac{S_j B_{t-s,j}^*}{\tilde{P}_j}$ and $\tilde{k}_{t-s,j} \equiv \frac{P_j^K K_{t-s,j}}{\tilde{P}_j}$.

Nominal wage income is $W_{t-s,j}$ and nominal taxes $T_{t-s,j}$; real wage income in

terms of the composite consumption good is $\tilde{w}_{t-s,j} \equiv \frac{W_{t-s,j}}{\tilde{P}_j}$ and real taxes is

$\tilde{\mathbf{t}}_{t-s,j} \equiv \frac{T_{t-s,j}}{\tilde{P}_j}$. We assume that the expected financial rates of return on all non-

monetary assets are equalised, that is,

$$1 + i_{j+1} = (1 + i_{j+1}^*) \frac{S_{j+1}}{S_j} \quad (5)$$

$$1 + i_j = \frac{1}{P_j^K} \left((1 - \mathbf{x}) P_{j+1}^K + \Omega_{j+1} \right) \quad (6)$$

We also assume that $(1 + \mathbf{d})^{-1}$ is not only the individual period probability of survival, but also the fraction of each age cohort, and therefore of the population as a whole, that survives till the next period. With efficient annuities markets, the gross nominal rate of return earned on government debt by survivors is therefore $(1 + i)(1 + \mathbf{d})$, and *mutatis mutandis* for all financial assets.

The household budget identity is

$$\begin{aligned}
& M_{t-s,t} + B_{t-s,t} + S_t B_{t-s,t}^* + P_t^K K_{t-s,t} \\
& \equiv (1+\mathbf{d}) \left(\begin{aligned} & (1+i_t^M)M_{t-s,t-1} + (1+i_t)B_{t-s,t-1} \\ & + (1+i_t^*)S_t B_{t-s,t-1}^* + [\Omega_t + (1-\mathbf{x})P_t^K]K_{t-s,t-1} \end{aligned} \right) \\
& + W_{t-s,t} - T_{t-s,t} - P_t C_{t-s,t}^H - S_t P_t^* C_{t-s,t}^F
\end{aligned} \tag{7}$$

Nominal notional household financial wealth, A , is defined as follows:

$$A_{t-s,t} \equiv M_{t-s,t} + B_{t-s,t} + S_t B_{t-s,t}^* + P_t^K K_{t-s,t}, \tag{8}$$

and real notional household financial wealth, $\tilde{a}_{t-s,t} \equiv \frac{A_{t-s,t}}{\tilde{P}_t}$

The period household budget identity (7) can, using equations (5) and (6), be rewritten as:

$$\tilde{a}_{t-s,t-1} \equiv \frac{1}{(1+\tilde{r}_t)(1+\mathbf{d})} \left(\begin{aligned} & \tilde{a}_{t-s,t} + \tilde{\mathbf{t}}_{t-s,t} - \tilde{w}_{t-s,t} + \frac{P_j}{\tilde{P}_j} c_{t-s,t}^H + \frac{S_t P_t^*}{\tilde{P}_t} c_{t-s,t}^F \\ & + \left(\frac{i_t - i_t^M}{1+\tilde{p}_t} \right) (1+\mathbf{d}) \tilde{m}_{t-s,t-1} \end{aligned} \right) \tag{9}$$

The household solvency constraint is

$$\lim_{N \rightarrow \infty} \prod_{s=t}^N \left(\frac{1}{(1+\tilde{r}_s)(1+\mathbf{d})} \right) \tilde{a}_{t-s,N} = 0 \tag{10}$$

The solvency constraint and the budget identity imply the following intertemporal budget constraint for the household of generation t - s :

$$\begin{aligned}
& \tilde{a}_{t-s,t-1} + \sum_{j=t}^{\infty} \prod_{s=t}^j \left(\frac{1}{(1+\tilde{r}_s)(1+\mathbf{d})} \right) (\tilde{w}_{t-s,j} - \tilde{\mathbf{t}}_{t-s,j}) \\
& \equiv \sum_{j=t}^{\infty} \prod_{s=t}^j \left(\frac{1}{(1+\tilde{r}_s)(1+\mathbf{d})} \right) \left[\begin{aligned} & \frac{P_j}{\tilde{P}_j} c_{t-s,j}^H + \frac{S_j P_j^*}{\tilde{P}_j} c_{t-s,j}^F \\ & + \left(\frac{i_j - i_j^M}{1+\tilde{p}_j} \right) (1+\mathbf{d}) \tilde{m}_{t-s,j-1} \end{aligned} \right]
\end{aligned} \tag{11}$$

From the first-order conditions we obtain the following:

For $q \neq 1$,

$$c^H = \mathbf{h} \left(\frac{P}{\bar{P}} \right)^{-q} \tilde{c} = \mathbf{h} \left[\mathbf{h} + (1-\mathbf{h}) \left(\frac{SP^*}{P} \right)^{1-q} \right]^{\frac{q}{1-q}} \tilde{c} \quad (12)$$

$$c^F = (1-\mathbf{h}) \left(\frac{SP^*}{\bar{P}} \right)^{-q} \tilde{c} = (1-\mathbf{h}) \left[\mathbf{h} \left(\frac{P}{SP^*} \right)^{1-q} + 1 - \mathbf{h} \right]^{\frac{q}{1-q}} \tilde{c} \quad (13)$$

For $q = 1$,

$$c^H = \mathbf{h} \left(\frac{P}{\bar{P}} \right)^{-1} \tilde{c} = \mathbf{h} \left(\frac{P}{SP^*} \right)^{h-1} \tilde{c} \quad (14)$$

$$c^F = (1-\mathbf{h}) \left(\frac{SP^*}{\bar{P}} \right)^{-1} \tilde{c} = (1-\mathbf{h}) \left(\frac{SP^*}{P} \right)^{-h} \tilde{c} \quad (15)$$

$$\tilde{m}_{t-s,j} = \left(\frac{1-\mathbf{a}}{\mathbf{a}} \right) \left(\frac{1+i_{j+1}}{i_{j+1} - i_{j+1}^M} \right)^j \tilde{c}_{t-s,j} \quad (16)$$

$$\begin{aligned} \frac{\tilde{c}_{t-s,j+1}}{\tilde{c}_{t-s,j}} &= \left(\frac{1+\tilde{r}_{j+1}}{1+\mathbf{r}} \right)^s \left(\frac{1 + \left(\frac{1-\mathbf{a}}{\mathbf{a}} \right) \left(\frac{1+i_{j+2}}{i_{j+2} - i_{j+2}^M} \right)^{j-1}}{1 + \left(\frac{1-\mathbf{a}}{\mathbf{a}} \right) \left(\frac{1+i_{j+1}}{i_{j+1} - i_{j+1}^M} \right)^{j-1}} \right)^{\frac{s-j}{j-1}} \quad \text{if } \mathbf{j} \neq 1 \\ &= \left(\frac{1+\tilde{r}_{j+1}}{1+\mathbf{r}} \right)^s \left(\frac{1+i_{j+2}}{i_{j+2} - i_{j+2}^M} \right)^{(s-1)(1-\mathbf{a})} \quad \text{if } \mathbf{j} = 1 \end{aligned} \quad (17)$$

We define *effective* real private financial wealth at the beginning of period t ,

$\tilde{f}_{t-s,t}$ as in (18). It allows for the fact that money carries an interest rate i_M rather than

i .

$$\begin{aligned} \tilde{f}_{t-s,t} &= (1+\tilde{r}_t)(1+\mathbf{d}) \left[\left(\frac{1+i_t^M}{1+i_t} \right) \tilde{m}_{t-s,t-1} + \tilde{b}_{t-s,t-s} + \tilde{b}_{t-s,t-1}^* + \tilde{k}_{t-s,t-1} \right] \\ &= (1+\tilde{r}_t)(1+\mathbf{d}) \left[\tilde{a}_{t-s,t-1} - \left(\frac{i_t - i_t^M}{1+i_t} \right) \tilde{m}_{t-s,t-1} \right] \end{aligned} \quad (18)$$

We also define real human wealth at the beginning of period t , $\tilde{h}(t-s, t)$, as follows:

$$\tilde{h}_{t-s,t} = \sum_{j=t}^{\infty} \prod_{s=t+1}^j \left(\frac{1}{(1+\tilde{r})_s(1+d)} \right) (\tilde{w}_{t-s,j} - \tilde{c}_{t-s,j}) \quad (19)^1$$

The first-order conditions (16) and (17), and the intertemporal budget constraint (18) imply the following consumption function for households born at time $t-s$ that survive till time t .

$$\tilde{c}_{t-s,t} = \tilde{m}_t (\tilde{f}_{t-s,t} + \tilde{h}_{t-s,t}) \quad (20)$$

If $j \neq 1$,

$\tilde{m}_t =$

$$\left\{ \sum_{j=t}^{\infty} \left[1 + \left(\frac{1-a}{a} \right) \left(\frac{1+i_{j+1}}{i_{j+1} - i_{j+1}^M} \right)^{j-1} \right] \prod_{s=t+1}^j \frac{(1+\tilde{r})_s^{s-1}}{(1+d)(1+r)^s} \left[\frac{1 + \left(\frac{1-a}{a} \right) \left(\frac{1+i_{s+1}}{i_{s+1} - i_{s+1}^M} \right)^{j-1}}{1 + \left(\frac{1-a}{a} \right) \left(\frac{1+i_s}{i_s - i_s^M} \right)^{j-1}} \right]^{\frac{s-j}{j-1}} \right\}^{-1} \quad (21)$$

When $j = 1$ (the elasticity of substitution between consumption and real money balances is unity, the marginal propensity to consume out of comprehensive wealth is

$$\tilde{m}_t \equiv a \left\{ \sum_{j=t}^{\infty} \prod_{s=t+1}^j \frac{(1+\tilde{r})_s^{s-1}}{(1+d)(1+r)^s} \left(\frac{1+i_{s+1}}{i_{s+1} - i_{s+1}^M} \right)^{(s-1)(1-a)} \right\}^{-1} \quad (22)$$

These expressions for the marginal propensity to consume out of comprehensive wealth simplify when future real and nominal interest rates are expected to be constant. In that case, (21) becomes

¹ We use the convention that $\prod_{s=t+1}^t x_s = 1$.

$$\tilde{\mathbf{m}} = \left[1 + \left(\frac{1-\mathbf{a}}{\mathbf{a}} \right) \left(\frac{1+i}{i-i^M} \right)^{j-1} \right]^{-1} \left[\frac{(1+\mathbf{d})(1+\mathbf{r})^s - (1+\tilde{r})^{s-1}}{(1+\mathbf{d})(1+\mathbf{r})^s} \right] \quad (23)$$

From equation (23), the *steady state* marginal propensity to consume out of comprehensive wealth is independent of the nominal interest rate if and only if the elasticity of substitution between consumption and real money balances is one ($\mathbf{j} = 1$). In that case the steady state marginal propensity to consume becomes

$$\tilde{\mathbf{m}} = \mathbf{a} \left[\frac{(1+\mathbf{d})(1+\mathbf{r})^s - (1+\tilde{r})^{s-1}}{(1+\mathbf{d})(1+\mathbf{r})^s} \right] \quad (24)$$

However, from equation (22), it is clear that $\mathbf{j} = 1$ is not sufficient for the marginal propensity to consume out of comprehensive wealth to be independent of the sequence of current and future nominal interest rates outside steady state. For that to be true we require both \mathbf{j} and \mathbf{s} , the intertemporal substitution elasticity, to be equal to unity (see Fischer [1979a,b]).

When $\mathbf{j} = \mathbf{s} = 1$ (logarithmic intertemporal preferences and a unitary elasticity of substitution between the composite consumption good and real money balances), the marginal propensity to consume out of comprehensive wealth simplifies to the expression given in equation (25) below. It is now also independent of the real interest rate.

$$\tilde{\mathbf{m}} = \mathbf{m} = \mathbf{a} \left(\frac{(1+\mathbf{r})(1+\mathbf{d}) - 1}{(1+\mathbf{r})(1+\mathbf{d})} \right) \quad (25)$$

Aggregation

Normalise population and labour force size at time 0 to be $L_0 = 1$. To every person alive in period t $\mathbf{b} \geq 0$ children are born. The size of the surviving cohort at

time t that was born at time $t-s$, $s \geq 0$ is $\mathbf{b}L_{t-s} \left(\frac{1}{1+\mathbf{d}} \right)^s = \mathbf{b}(1+\mathbf{b})^{t-s} \left(\frac{1}{1+\mathbf{d}} \right)^t$.² For any individual agent's stock or flow variable, $Y_{t-s,t}$, we define the corresponding population aggregate Y_t as follows:

$$\begin{aligned} Y_t &\equiv \sum_{s=1}^{\infty} \mathbf{b}(1+\mathbf{b})^{t-s} \left(\frac{1}{1+\mathbf{d}} \right)^t Y_{t-s,t} & \mathbf{b} > 0 \\ &\equiv Y_0 \left(\frac{1}{1+\mathbf{d}} \right)^t & \mathbf{b} = 0 \end{aligned} \quad (26)^3$$

We also assume that each surviving household, regardless of age, earns the same wage income and pays the same taxes, that is,

$$W_{t-s,t} = W_t, \quad s \geq 0 \quad (27)$$

and

$$T_{t-s,t} = T_t, \quad s \geq \bar{0} \quad (28)$$

It follows that each surviving household has the same human wealth:

$$\tilde{h}_{t-s,t} = \tilde{h}_t, \quad s \geq 0 \quad (29)$$

Finally, we assume that people are born with zero non-human wealth, that is,

$$\tilde{a}_{t,t} = 0 \quad (30)$$

It follows that aggregate consumption is given by

For $\mathbf{q} \neq 1$,

$$c^H = \mathbf{h} \left(\frac{P}{\tilde{P}} \right)^{-\mathbf{q}} \tilde{c} = \mathbf{h} \left[\mathbf{h} + (1-\mathbf{h}) \left(\frac{SP^*}{P} \right)^{1-\mathbf{q}} \right]^{\frac{\mathbf{q}}{1-\mathbf{q}}} \tilde{c} \quad (31)$$

² $L_{t+1} = \left(\frac{1+\mathbf{b}}{1+\mathbf{d}} \right) L_t$.

³ Y_0 is assumed to be exogenously given if $\mathbf{b} = 0$.

$$c^F = (1-h) \left(\frac{SP^*}{\tilde{P}} \right)^{-q} \tilde{c} = (1-h) \left[h \left(\frac{P}{SP^*} \right)^{1-q} + 1-h \right]^{\frac{q}{1-q}} \tilde{c} \quad (32)$$

For $q=1$,

$$c^H = h \left(\frac{P}{\tilde{P}} \right)^{-1} \tilde{c} = h \left(\frac{P}{SP^*} \right)^{h-1} \tilde{c} \quad (33)$$

$$c^F = (1-h) \left(\frac{SP^*}{\tilde{P}} \right)^{-1} \tilde{c} = (1-h) \left(\frac{SP^*}{P} \right)^{-h} \tilde{c} \quad (34)$$

$$\tilde{c}_t = \tilde{\mathbf{m}} (f_t + \tilde{h}_t) \quad (35)$$

$$\tilde{f}_t = [1 + r_t] \left[\tilde{a}_{t-1} - \left(\frac{i_t - i_t^M}{1 + i_t} \right) \tilde{m}_{t-1} \right] \quad (36)$$

$$\tilde{a}_{t-1} \equiv \frac{1}{[1 + \tilde{r}_t]} \left(\tilde{a}_t + \tilde{\mathbf{t}}_t - \tilde{w}_t + \frac{P_j}{\tilde{P}_j} c_t^H + \frac{S_t P_t^*}{\tilde{P}_t} c_t^F + \left(\frac{i_t - i_t^M}{1 + \tilde{\mathbf{p}}_t} \right) \tilde{m}_{t-1} \right) \quad (37)$$

$$\tilde{h}_t = \sum_{j=t}^{\infty} \prod_{s=t+1}^j \left(\frac{1}{(1 + \tilde{r}_s)(1 + \mathbf{b})} \right) (\tilde{w}_j - \tilde{\mathbf{t}}_j) \quad (38)$$

$$\tilde{m}_t = \left(\frac{1 - \mathbf{a}}{\mathbf{a}} \right) \left(\frac{1 + i_{t+1}}{i_{t+1} - i_{t+1}^M} \right)^j \tilde{c}_t \quad (39)$$

$$\tilde{a}_t \equiv \tilde{m}_t + \tilde{b}_t + \tilde{b}_t^* + \tilde{k}_t \equiv \frac{M_t + B_t + S_t B_t^* + P_t^K K_t}{\tilde{P}_t} \quad (40)$$

, where M is the aggregate nominal base money stock, B the aggregate stock of non-monetary nominal government debt, B^* the aggregate stock of net foreign assets (denominated in foreign currency) held by the private sector and K the domestic capital stock. As we assume that the physical resources owned by households consist of their labour endowment and the domestic capital stock, which are both used exclusively in the production of domestic output, it is helpful, in order to identify the

effect of changes in international relative prices, to rewrite equations (35) to (40) using domestic output rather than the composite consumption good as the numéraire.

For any stock variable, e.g. the capital stock, we define

$$k_t \equiv \frac{P_{t-1}^K K_t}{P_{t-1}} = \frac{\tilde{P}_{t-1}}{P_{t-1}} \tilde{k}_t. \quad \text{For any flow variable, e.g. consumption of the composite}$$

commodity, we define $c_t \equiv \frac{\tilde{P}_t}{P_t} \tilde{c}_t$. The inflation rate of domestic output is \mathbf{p} , that is,

$$1 + \mathbf{p}_t \equiv \frac{P_t}{P_{t-1}}. \quad \text{The real interest rate in terms of domestic output is } r, \text{ that is,}$$

$$1 + r_t \equiv (1 + i_t) \frac{P_{t-1}}{P_t} = \frac{1 + i_t}{1 + \mathbf{p}_t} = (1 + \tilde{r}_t) \left(\frac{1 + \tilde{\mathbf{p}}_t}{1 + \mathbf{p}_t} \right).$$

This yields the following aggregate consumption behaviour:

For $\mathbf{q} \neq 1$,

$$c^H = \mathbf{h} \left(\frac{P}{\tilde{P}} \right)^{1-\mathbf{q}} c = \mathbf{h} \left[\mathbf{h} + (1-\mathbf{h}) \left(\frac{SP^*}{P} \right)^{1-\mathbf{q}} \right]^{-1} c \quad (41)$$

$$c^F = (1-\mathbf{h}) \left(\frac{SP^*}{\tilde{P}} \right)^{-\mathbf{q}} \frac{P}{\tilde{P}} c = (1-\mathbf{h}) \left[\mathbf{h} \left(\frac{SP^*}{P} \right)^{\mathbf{q}} + (1-\mathbf{h}) \frac{SP^*}{P} \right]^{-1} c \quad (42)$$

For $\mathbf{q} = 1$,

$$c^H = \mathbf{h}c \quad (43)$$

$$c^F = (1-\mathbf{h}) \left(\frac{SP^*}{P} \right)^{-1} c \quad (44)$$

$$c_t = \mathbf{m}_t (f_t + h_t) \quad (45)$$

$\mathbf{m} \equiv$

$$\left\{ \sum_{j=t}^{\infty} \left[1 + \left(\frac{1-a}{a} \right) \left(\frac{1+i_{j+1}}{i_{j+1} - i_{j+1}^M} \right)^{j-1} \right] \prod_{s=t+1}^j \frac{(1+r_s)^{s-1}}{(1+d)(1+r)^s} \left[\frac{1 + \left(\frac{1-a}{a} \right) \left(\frac{1+i_{s+1}}{i_{s+1} - i_{s+1}^M} \right)^{j-1}}{1 + \left(\frac{1-a}{a} \right) \left(\frac{1+i_s}{i_s - i_s^M} \right)^{j-1}} \right]^{\frac{s-j}{j-1}} \right\}^{-1} \quad (46)$$

$$a_t \equiv (1+r)_t a_{t-1} + w_t - \mathbf{t}_t - c_t - (j - i^M) \frac{m_{t-1}}{1+p_t} \quad (47)$$

$$h_t = \sum_{j=t}^{\infty} \prod_{s=t+1}^j \left(\frac{1}{(1+r)(1+b)} \right) (w_j - \mathbf{t}_j) \quad (48)$$

$$m_t = \left(\frac{1-a}{a} \right) \left(\frac{1+i_{t+1}}{i_{t+1} - i_{t+1}^M} \right)^j c_t \quad (49)$$

$$f_t = (1+r_t) \left(a_{t-1} - \left(\frac{i_t - i_t^M}{1+i_t} \right) m_{t-1} \right) \quad (50)$$

$$a_t \equiv m_t + b_t + b_t^* + k_t \equiv \frac{M_t + B_t + S_t B_t^* + P_t^K K_t}{P_t} \quad (51)$$

Government

The government (that is, the consolidated central bank and general government sector) spends g^H on domestic output, g^F on foreign output, raises taxes T in nominal terms, issues base money with a nominal interest rate i^H , domestic currency debt with a nominal interest rate i and holds foreign exchange reserves D^* . We shall call $SD^* - B - M$ the financial net worth of the government.

$$\begin{aligned} & M_t + B_t - S_t D_t^* \\ & \equiv P g_t^H + S_t P_t g_t^F - T_t \\ & + (1+i_t^M) M_{t-1} + (1+i_t) B_{t-1} - S_t (1+i_t^*) D_{t-1}^* \end{aligned} \quad (52)$$

Letting $\tilde{g} \equiv \frac{P g^H + S P^* g^F}{\tilde{P}}$ and $\tilde{d}^* \equiv \frac{SD^*}{\tilde{P}}$, we can rewrite equation (52) as

$$\begin{aligned} & \tilde{b}_t + \tilde{m}_t - \tilde{d}_t^* \\ & \equiv (1 + \tilde{r}_t)(\tilde{b}_{t-1} + \tilde{m}_{t-1} - \tilde{d}_{t-1}^*) + \tilde{g}_t - \tilde{\tau}_t + \frac{(i_t^M - i_t)}{1 + \tilde{\mathbf{p}}_t} \tilde{m}_{t-1}. \end{aligned}$$

Slightly more useful, for when below we ‘internalise’ the government’s intertemporal budget constraint by substituting it into the household intertemporal budget constraint is the following representation:

$$\tilde{b}_t - \tilde{d}_t^* \equiv (1 + \tilde{r}_t)(\tilde{b}_{t-1} - \tilde{d}_{t-1}^*) + \tilde{g}_t - \tilde{\tau}_t + \left(\frac{i_t^M}{1 + \tilde{\mathbf{p}}_t} \right) \tilde{m}_{t-1} - \frac{\Delta M_t}{\tilde{P}_t} \quad (53)^4$$

With the usual no-Ponzi finance solvency constraint:

$$\lim_{j \rightarrow \infty} \prod_{s=t}^j \left(\frac{1}{1 + \tilde{r}_s} \right) (\tilde{b}_j - \tilde{d}_j^*) = 0 \quad (54)$$

Note that it is the present discounted value of the government’s terminal non-monetary debt that must be zero. There is no requirement for the government to pay off (even in present value terms) its monetary debt.

This yields the government’s intertemporal budget constraint:

$$\begin{aligned} (1 + \tilde{r}_t)(\tilde{b}_{t-1} - \tilde{d}_{t-1}^*) &= \frac{(1 + i_t)B_{t-1} - (1 + i_t^*)S_t D_{t-1}^*}{P_t} \\ &= \sum_{j=t}^{\infty} \prod_{s=t+1}^j \left(\frac{1}{1 + \tilde{r}_s} \right) \left(\tilde{\tau}_j - \tilde{g}_j - \frac{i_j^M}{1 + \tilde{\mathbf{p}}_j} \tilde{m}_{j-1} + \frac{\Delta M_j}{\tilde{P}_j} \right) \end{aligned} \quad (55)$$

We assume that government spending on goods and services is determined, analogously to private consumption. With $0 < \hat{\mathbf{h}} < 1$; $\hat{\mathbf{q}} > 0$,

$$\begin{aligned} g^H &= \hat{\mathbf{h}} \left(\frac{P}{\tilde{P}} \right)^{-\hat{\mathbf{q}}} \tilde{g} = \hat{\mathbf{h}} \left[\hat{\mathbf{h}} + (1 - \hat{\mathbf{h}}) \left(\frac{SP^*}{P} \right)^{1-\hat{\mathbf{q}}} \right]^{\frac{\hat{\mathbf{q}}}{1-\hat{\mathbf{q}}}} \tilde{g} && \text{if } \hat{\mathbf{q}} \neq 1 \\ &= \hat{\mathbf{h}} \left(\frac{P}{\tilde{P}} \right)^{-1} \tilde{g} = \hat{\mathbf{h}} \left(\frac{P}{SP^*} \right)^{\hat{\mathbf{h}}-1} \tilde{g} && \text{if } \hat{\mathbf{q}} = 1 \end{aligned} \quad (56)$$

⁴ $\Delta M_{t+1} \equiv M_{t+1} - M_t$

$$\begin{aligned}
g^F &= (1-\hat{\mathbf{h}}) \left(\frac{SP^*}{\tilde{P}} \right)^{-\hat{\mathbf{q}}} \tilde{g} = (1-\hat{\mathbf{h}}) \left[\hat{\mathbf{h}} \left(\frac{P}{SP^*} \right)^{1-\hat{\mathbf{q}}} + 1-\hat{\mathbf{h}} \right]^{\frac{\hat{\mathbf{q}}}{1-\hat{\mathbf{q}}}} \tilde{g} && \text{if } \hat{\mathbf{q}} \neq 1 \\
&= (1-\hat{\mathbf{h}}) \left(\frac{SP^*}{\tilde{P}} \right)^{-1} \tilde{g} = (1-\hat{\mathbf{h}}) \left(\frac{SP^*}{P} \right)^{-\hat{\mathbf{h}}} \tilde{g} && \text{if } \hat{\mathbf{q}} = 1 \quad (57)
\end{aligned}$$

As the government's endowment stream (the tax base) consists of domestic output, we assume that government spending decisions can be represented by an exogenous sequence of aggregate public spending measured in domestic output, $\{g_j; j \geq t\}$ with $g = \frac{\tilde{P}}{P} \tilde{g}$. International relative prices then distribute this aggregate

across domestic goods and imports according to equation (56), that is

$$\begin{aligned}
g^H &= \hat{\mathbf{h}} \left(\frac{P}{\tilde{P}} \right)^{1-\hat{\mathbf{q}}} g = \hat{\mathbf{h}} \left[\hat{\mathbf{h}} + (1-\hat{\mathbf{h}}) \left(\frac{SP^*}{P} \right)^{1-\hat{\mathbf{q}}} \right]^{-1} g && \text{if } \hat{\mathbf{q}} \neq 1 \\
&= \hat{\mathbf{h}} g && \text{if } \hat{\mathbf{q}} = 1 \quad (58)
\end{aligned}$$

$$\begin{aligned}
g_F &= (1-\hat{\mathbf{h}}) \left(\frac{SP^*}{\tilde{P}} \right)^{-\hat{\mathbf{q}}} \frac{P}{\tilde{P}} g = (1-\hat{\mathbf{h}}) \left(\hat{\mathbf{h}} \left(\frac{SP^*}{P} \right)^{\hat{\mathbf{q}}} + (1-\hat{\mathbf{h}}) \frac{SP^*}{P} \right)^{-1} g && \text{if } \hat{\mathbf{q}} \neq 1 \\
&= (1-\hat{\mathbf{h}}) \left(\frac{SP^*}{P} \right)^{-1} g && \text{if } \hat{\mathbf{q}} = 1 \quad (59)
\end{aligned}$$

We can substitute the government's intertemporal budget constraint given in (55) into the private consumption function (45), using (48) and (51). This yields

$$c_t = \mathbf{m} \left\{ \begin{aligned} & \left[\frac{(M_{t-1} + (1+i_t^*)S_t[B_{t-1}^* + D_{t-1}^*]) + ((1-\mathbf{x})P_t^K + \Omega_t)K_{t-1}}{P_t} \right. \\ & + \sum_{j=t}^{\infty} \left[\prod_{s=t+1}^j \left(\frac{1}{(1+r_s)(1+\mathbf{b})} \right) w_j - \prod_{s=t+1}^j \left(\frac{1}{1+r_s} \right) g_j \right] \\ & + \sum_{j=t}^{\infty} \left[\prod_{s=t+1}^j \left(\frac{1}{1+r_s} \right) - \prod_{s=t+1}^j \left(\frac{1}{(1+r_s)(1+\mathbf{b})} \right) \right] \mathbf{t}_j \\ & + \sum_{j=t}^{\infty} \left[\prod_{s=t+1}^j \left(\frac{1}{1+r_s} \right) \left(\frac{\Delta M_j}{P_j} \right) \right] \\ & - \sum_{j=t+1}^{\infty} \left[\prod_{s=t+1}^j \left(\frac{1}{1+r_s} \right) \left(\frac{i_j^M m_{j-1}}{1+\mathbf{p}_j} \right) \right] \end{aligned} \right\} \quad (60)$$

Equation (60) represents aggregate consumption behaviour when all consumers are permanent income consumers. If, instead, a fraction \mathbf{I} of households always consume their current disposable income (and therefore always possesses zero financial net worth), aggregate consumption would be given by:

$$c_t = \mathbf{m} \left\{ \begin{aligned} & \left[\frac{(M_{t-1} + (1+i_t^*)S_t[B_{t-1}^* + D_{t-1}^*]) + ((1-\mathbf{x})P_t^K + \Omega_t)K_{t-1}}{P_t} \right. \\ & + \sum_{j=t}^{\infty} \left[(1-\mathbf{I}) \prod_{s=t+1}^j \left(\frac{1}{(1+r_s)(1+\mathbf{b})} \right) w_j - \prod_{s=t+1}^j \left(\frac{1}{1+r_s} \right) g_j \right] \\ & + \sum_{j=t}^{\infty} \left[\prod_{s=t+1}^j \left(\frac{1}{1+r_s} \right) - (1-\mathbf{I}) \prod_{s=t+1}^j \left(\frac{1}{(1+r_s)(1+\mathbf{b})} \right) \right] \mathbf{t}_j \\ & + \sum_{j=t}^{\infty} \left[\prod_{s=t+1}^j \left(\frac{1}{1+r_s} \right) \left(\frac{\Delta M_j}{P_j} \right) \right] \\ & - \sum_{j=t+1}^{\infty} \left[\prod_{s=t+1}^j \left(\frac{1}{1+r_s} \right) \left(\frac{i_j^M m_{j-1}}{1+\mathbf{p}_j} \right) \right] \end{aligned} \right\} + \mathbf{I}(w_t - \mathbf{t}_t) \quad (61)$$

If only permanent income households hold money balances, the demand for money becomes

$$m_t = \left(\frac{1-a}{a} \right) \left(\frac{1+i_{t+1}}{i_{t+1} - i_{t+1}^M} \right)^j [c_t - I(w_t - t_t)] \quad (62)$$

$$i \geq i^M$$

Private Investment

A competitive firm hires labour L and invests in a composite investment good $\tilde{\mathbf{i}}$ each period to maximise the present discounted value of its future cash-flow, shown in equation (63), subject to the capital stock dynamics given in equation (64). The production function is constant returns to scale in capital, K , and labour, L , has positive but diminishing marginal products of capital and labour, is strictly concave and satisfies the Inada conditions. There are quadratic adjustment costs associated with investment, and the adjustment cost function is constant returns to scale. The money wage is \mathbf{w} and \tilde{P}^t is the price of the composite investment good. Θ is the level of total factor productivity and \mathbf{x} is the proportional depreciation rate of the capital stock.

$$\sum_{j=t}^{\infty} \prod_{s=t+1}^j \left(\frac{1}{1+i_s} \right) \left[P_j \left(\Theta_j F[K_j, L_j] - \frac{1}{2} v \frac{(\tilde{\mathbf{i}}_j)^2}{K_j} \right) - \mathbf{w}_j L_j \right] \quad (63)$$

$$\left[-\tilde{P}_j^t \tilde{\mathbf{i}}_j \right]$$

$$v > 0$$

$$K_t = K_{t-1} \frac{1}{1+\mathbf{x}} + \tilde{\mathbf{i}}_t \quad (64)$$

$$1 \geq \mathbf{x} \geq 0$$

$$\tilde{\mathbf{i}} = \left(\bar{\mathbf{h}}^{\frac{1}{\bar{\mathbf{q}}}} \bar{\mathbf{i}}_H^{\frac{\bar{\mathbf{q}}-1}{\bar{\mathbf{q}}}} + (1-\bar{\mathbf{h}})^{\frac{1}{\bar{\mathbf{q}}}} \bar{\mathbf{i}}_F^{\frac{\bar{\mathbf{q}}-1}{\bar{\mathbf{q}}}} \right)^{\frac{\bar{\mathbf{q}}}{\bar{\mathbf{q}}-1}}$$

$$1 > \bar{\mathbf{h}} > 0; \bar{\mathbf{q}} > 0; \bar{\mathbf{q}} \neq 1$$

or, if $\bar{\mathbf{q}} = 1$

$$\tilde{\mathbf{i}} = \bar{\mathbf{i}}_H^{\bar{\mathbf{h}}} \bar{\mathbf{i}}_F^{1-\bar{\mathbf{h}}}$$

$$\tilde{P}_t = \left[\bar{\mathbf{h}} P^{1-\bar{\mathbf{q}}} + (1-\bar{\mathbf{h}}) (SP^*)^{1-\bar{\mathbf{q}}} \right]^{\frac{1}{1-\bar{\mathbf{q}}}} \quad \text{if } \bar{\mathbf{q}} \neq 1$$

$$= P^{\bar{\mathbf{h}}} (SP^*)^{1-\bar{\mathbf{h}}} \quad \text{if } \bar{\mathbf{q}} = 1$$

The optimal investment rules are as follows:

$$\tilde{\mathbf{i}}_t = \frac{1}{v} \left[\frac{P_t^K - \tilde{P}_t^I}{P_t} \right] K_{t-1}$$

$$= \frac{1}{v} \left[\frac{P_t^K}{P_t} - \left[\bar{\mathbf{h}} + (1-\bar{\mathbf{h}}) \left(\frac{S_t P_t^*}{P_t} \right)^{1-\bar{\mathbf{q}}} \right]^{\frac{1}{1-\bar{\mathbf{q}}}} \right] K_{t-1} \quad \text{if } \bar{\mathbf{q}} \neq 1$$

$$= \frac{1}{v} \left[\frac{P_t^K}{P_t} - \left(\frac{S_t P_t^*}{P_t} \right)^{1-\bar{\mathbf{h}}} \right] K_{t-1} \quad \text{if } \bar{\mathbf{q}} = 1$$

$$\frac{P_t^K}{P_t} = \sum_{j=t}^{\infty} \prod_{s=t+1}^j \left(\frac{1}{(1+r_s)(1+\mathbf{x})} \right) \left[\Theta_j F_K(K_j, L_j) + \frac{1}{2} v \left(\frac{\tilde{\mathbf{i}}_j}{K_j} \right)^2 \right]$$

$$\mathbf{w}_j = P_j \Theta_j F_L(K_j, L_j)$$

Let $\mathbf{i} \equiv \frac{\tilde{P}^I}{P} \tilde{\mathbf{i}}$ denote investment measured in units of domestic output, then

$$\mathbf{i}_t = \frac{1}{v} \left(\frac{P_t^K}{\tilde{P}_t^I} - 1 \right) K_{t-1}$$

$$= \frac{1}{v} \left[\frac{P_t^K}{P_t} \left[\bar{\mathbf{h}} + (1-\bar{\mathbf{h}}) \left(\frac{S_t P_t^*}{P_t} \right)^{1-\bar{\mathbf{q}}} \right]^{\frac{1}{\bar{\mathbf{q}}-1}} - 1 \right] K_{t-1} \quad \text{if } \bar{\mathbf{q}} \neq 1$$

$$= \frac{1}{v} \left[\frac{P_t^K}{P_t} \left(\frac{S_t P_t^*}{P_t} \right)^{\bar{\mathbf{h}}-1} - 1 \right] K_{t-1} \quad \text{if } \bar{\mathbf{q}} = 1$$

$$\frac{P_t^k}{P_t} = \sum_{j=t}^{\infty} \prod_{s=t+1}^j \left(\frac{1}{(1+r_s)(1+\mathbf{x})} \right) \left[\Theta_j F_K(K_j, L_j) + \frac{1}{2} v \left(\frac{\mathbf{i}_j}{K_j} \right)^2 \right] \quad (71)$$

If $\hat{q} \neq 1$

$$\begin{aligned} \mathbf{i}^H &= \bar{\mathbf{h}} \left(\frac{P}{\tilde{P}^I} \right)^{1-\bar{q}} \mathbf{i} = \bar{\mathbf{h}} \left[\bar{\mathbf{h}} + (1-\bar{\mathbf{h}}) \left(\frac{SP^*}{P} \right)^{1-\bar{q}} \right]^{-1} \mathbf{i} \\ \mathbf{i}^F &= (1-\bar{\mathbf{h}}) \left(\frac{SP^*}{\tilde{P}^I} \right)^{-\bar{q}} \mathbf{i} = (1-\bar{\mathbf{h}}) \left[\bar{\mathbf{h}} \left(\frac{P}{SP^*} \right)^{\bar{q}} + (1-\bar{\mathbf{h}}) \frac{P}{SP^*} \right]^{-1} \mathbf{i} \end{aligned} \quad (72)$$

$$0 < \bar{\mathbf{h}} < 1; \bar{q} > 0$$

Note that $w = \frac{wL}{P}$ and $\Omega = P \left[\Theta F_K(K, L) + \frac{1}{2} v \left(\frac{\mathbf{i}}{K} \right)^2 \right]$.

Export demand

Without modelling the rest of the world in any detail, we want to specify export demand for domestic output, x , analogously to the home country import demand functions for private consumption, public spending and private investment. We assume that if all factors of production that produce foreign output (and none of the factors of production that produce domestic output) are owned by foreigners, and that aggregate demand in the rest of the world is for a composite commodity whose ideal consumer price index is \tilde{P}^* , where

$$\tilde{P}^* = \left[\mathbf{h}^* P^{*(1-q^*)} + (1-\mathbf{h}^*) \left(\frac{P}{S} \right)^{1-q^*} \right]^{\frac{1}{1-q^*}} \quad \text{if } q^* \neq 1 \quad \text{and } \tilde{P}^* = P^{*h^*} \left(\frac{P}{S} \right)^{1-h^*} \quad \text{if } q^* = 1. \quad \text{Finally,}$$

we assume that the small home country takes aggregate rest-of-the-world demand measured in foreign output, $\mathbf{z}^* > 0$, as given. The export demand for home country output are:

$$\begin{aligned} x &= (1-\mathbf{h}^*) \left[\mathbf{h}^* \left(\frac{P}{SP^*} \right)^{q^*} + (1-\mathbf{h}^*) \frac{P}{SP^*} \right]^{-1} \mathbf{z}^* && \text{if } q^* \neq 1 \\ &= (1-\mathbf{h}^*) \frac{SP^*}{P} \mathbf{z}^* && \text{if } q^* = 1 \end{aligned} \quad (73)$$

Completing the model with some simple wage-price dynamics

The paper only considers the demand-side of the model. For completeness a sketch of a fairly New-Keynesian wage-price block is appended here. The nominal wage in period t is predetermined. Output is demand-determined and employment is determined by output, y , and the production function:

$$e = y = \Theta F(K, L) \quad (74)$$

Money wage determination follows a two-period staggered overlapping wage setting model in the spirit of Taylor [1979, 1980]. Instead of Taylor's relative *money* wage model, we use Buiter and Jewitt's overlapping *real* wage specification (Buiter and Jewitt [1981]). Half the labour force negotiates a two-period nominal contract wage each period. For instance, in period $t-1$, the nominal contract wage for periods t and $t+1$ is negotiated. The nominal contract period negotiated in period $t-1$ aims to achieve a given average real wage in periods t and $t+1$. That real wage depends on expected demand pressure in the labour market in the next two periods (proxied by the output gap, $y - \bar{y}$ over the life of the contract) and on the real wages achieved under the money wage contracts with which the contract negotiated in period $t-1$ overlaps. Let $c(t)$ denote the logarithm of the nominal contract wage negotiated in period $t-1$ for periods t and $t+1$. Unlike in the rest of the paper, we include the conditional expectation operator \mathbf{e}_{t-1} explicitly, to underline the fact that the period t nominal contract wage is indeed predetermined.

$$\begin{aligned} & c_t - \frac{1}{2} \mathbf{e}_{t-1} (\ln \tilde{P}_t + \ln \tilde{P}_{t+1}) \\ & = \mathbf{y} \mathbf{e}_{t-1} (y_t - \bar{y}_t + y_{t+1} - \bar{y}_{t+1}) + \mathbf{z} \mathbf{e}_{t-1} \left(c_{t-1} - \frac{1}{2} (\ln \tilde{P}_{t-1} + \ln \tilde{P}_t) \right) \\ & + (1 - \mathbf{z}) \mathbf{e}_{t-1} \left(c_{t+1} - \frac{1}{2} (\ln \tilde{P}_{t+1} + \ln \tilde{P}_{t+2}) \right) \\ & \mathbf{y} > 0, 0 \leq \mathbf{z} \leq 1 \end{aligned} \quad (75)$$

The money wage in period t , W_t , is the average of the contract wages negotiated in the previous two periods.

$$\ln W_t \equiv \frac{1}{2}(c_t + c_{t-1}) \quad (76)$$

Let \bar{L} be the exogenous labour supply, then capacity output \bar{y} is given by:

$$\bar{y} = \Theta F(K, \bar{L}) \quad (77)$$

The price of domestic output can either be derived from the condition that the marginal product of labour equals the real product wage (equation (78)) or by the mark-up rule in equation (79) specifying the price of domestic output as a constant proportional mark-up on unit labour cost.

$$P = W (\Theta F_L(K, L))^{-1} \quad (78)$$

$$P = \Psi \left(\frac{WL}{Y} \right) \quad \Psi > 1 \quad (79)$$

References

Buiter, Willem H. [2003], "Deflation: Prevention and Cure", NBER Working Paper No. 9623, April. Latest version at <http://www.nber.org/~wbuiter/def.pdf> .

Buiter, Willem H. and Ian Jewitt [1981], "Staggered wage setting with real wage relativities: variations on a theme of Taylor", *Manchester School*, 49, pp. 211-28, reprinted in Willem H. Buiter, *Macroeconomic Theory and Stabilization Policy*, Manchester University Press, University of Michigan Press, 1989, pp. 183-199.

Fischer, Stanley [1979a], "'Anticipations and the Non-Neutrality of Money," *Journal of Political Economy*, April, 225-52.

Fischer, Stanley [1979b], "Capital Accumulation on the Transition Path in a Monetary Optimizing Model," *Econometrica*, November, 1433-40.

Taylor, John B [1979], "Staggered Wage Setting in a Macro Model", *American Economic Review*, Vol. 69, No. 2, pp. 108-113.

Taylor, John B. [1980], "Aggregate Dynamics and Staggered Contracts", *Journal of Political Economy*, Vol. 88, No.1, pp. 1-23..